Please write clearly in block capitals.

Centre number |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- |

Candidate number


Surname
Forename(s)
Candidate signature

## GCSE

## Mathematics

Higher


## Summer 2019

Time allowed: 1 hour 30 minutes

## Materials

For this paper you must have:

- a calculator
- mathematical instruments.



## Instructions

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Answer all questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- Do all rough work in this book. Cross through any work you do not want to be marked.


## Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80 .
- You may ask for more answer paper, graph paper and tracing paper. These must be tagged securely to the answer book.


## Advice

- In all calculations, show clearly how you work out your answer.

| For Examiner's Use |  |
| :---: | :---: |
| Pages | Mark |
| 3 |  |
| $4-5$ |  |
| $6-7$ |  |
| $8-9$ |  |
| $10-11$ |  |
| $12-13$ |  |
| $14-15$ |  |
| $16-17$ |  |
| $18-19$ |  |
| $20-21$ |  |
| $22-23$ |  |
| $24-25$ |  |
| $26-27$ |  |
| TOTAL |  |

## Practice Paper Overview

| Q | Topic | Mark | Total |
| :--- | :--- | :---: | :---: |
| 1 | Angles in Polygons | 1 |  |
| 2 | Algebraic Factors | 1 |  |
| 3 | Factorise and Solve | 1 |  |
| 4 | Congruence | 2 |  |
| 5 | Percentage Change | 2 |  |
| 6 | Scatter Graph | 4 |  |
| 7 | Quadratic Graph | 7 |  |
| 8 | Compound Interest | 5 |  |
| 9 | Product of Prime Factors | 3 |  |
| 10 | Sine Rule MCQ | 1 |  |
| 11 | Pie Chart | 4 |  |
| 12 | Angles on Parallel Lines | 3 |  |
| 13 | Form and Solve Inequalities | 3 |  |
| 14 | Reverse Averages | 3 |  |
| 15 | Direct Proportion | 2 |  |
| 16 | Combined Transformations | 4 |  |
| 17 | Algebraic Ratio | 4 |  |
| 18 | Circle Theorem MCQ | 1 |  |
| 19 | Perpendicular Lines | 3 |  |
| 20 | Probability Problem | 4 |  |
| 21 | Quadratic Formula | 5 |  |
| 22 | Iteration | 3 |  |
| 23 | Rearranging Equations | 3 |  |
| 24 | $3 D$ Pythagoras | 4 |  |
| 25 | Cosine Rule | 4 |  |
| 26 | Algebraic Fractions |  | 80 |
|  |  |  |  |
|  |  | Total |  |

1 A shape has an interior angle of $120^{\circ}$.
How many sides does the shape have?

2 Circle the Highest Common Factor (HCF) of $12 x y^{3}$ and $18 x^{3} y^{9}$
$2 x y^{3}$
$3 x^{3} y^{9}$
$3 x^{3} y$
$6 x y^{3}$
$6 x^{3} y^{9}$
$36 x y^{9}$

3 Circle the solutions to $x^{2}-5 x-24=0$

$$
\begin{array}{ll}
x=-6 \text { and } x=4 & x=-4 \text { and } x=6 \\
x=-3 \text { and } x=8 & x=-8 \text { and } x=3
\end{array}
$$

4 Here are four triangles
Not drawn


8 cm


B


D


4 (a) Which two triangles are congruent? Circle your answers.
A
B
C
D

4 (b) Circle the reason for your answer to part (a).

SSS
ASA
SAS
RHS

> ASA

SAS


5 Paul buys a laptop from PC World for $£ 529$.
A year later it is worth $£ 444.36$.
Calculate the percentage decrease in the price.
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$
6 Below is a scatter graph showing the air temperature and the height above sea level.


6 (a) Describe the correlation between the air temperature and the height above sea level.
$\qquad$
$\qquad$
6 (b) Circle and write down the coordinates of the outlier.

Answer $\qquad$
6 (c) Find an estimate of the height above sea level when the air temperature is $-3^{\circ} \mathrm{C}$.
$\qquad$
Answer $\qquad$

7 (a) Complete the table of values for $y=x^{2}+4 x-3$.

| $\boldsymbol{x}$ | -4 | -3 | -2 | -1 | 0 | 1 | 2 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{y}$ | -3 |  | -7 | -6 |  | 2 |  |

7 (b) On the gird, draw the graph of $y=x^{2}+4 x-3$.


7 (c) Circle the coordinates of the turning point of the curve.
$(0,-3)$
$(-2,-7)$
$(-2,1)$
$(2,-7)$
$(4,-3)$

7 (d) Use the graph to find approximate solutions to $x^{2}+4 x-3=-5$
[2 marks]
$\qquad$
$\qquad$
$x=$ $\qquad$ $x=$ $\qquad$

8 The value of a new house $£ V$ is given by

$$
V=160000 \times 1.014^{t}
$$

where $t$ is the age of house in complete years.


8 (a) Write down the value of V when $t=0$.
$\qquad$
$\qquad$
Answer $\qquad$
8 (b) What is the value of $V$ after 3 years?
$\qquad$
$\qquad$

Answer $\qquad$
8 (c) After how many complete years will the house's value rise above £180 000?
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$

9 Express 1176 as a product of its prime factors in index form.

## Answer

10 Which equations gives the missing length, $x$, of this triangle?


Circle your answer.

$$
\begin{array}{ll}
\frac{x}{\sin (50)}=\frac{12}{\sin (70)} & \frac{x}{\sin (50)}=\frac{12}{\sin (14)} \\
\frac{x}{\sin (70)}=\frac{12}{\sin (50)} & \frac{x}{\sin (70)}=\frac{14}{\sin (70)}
\end{array}
$$

11 The pie chart shows some information about the medals the
United States received at the Rio Olympics in 2016.


United States
Medal Results


The angle for gold would be $24^{\circ}$ more than the angle for Silver.
There were 120 medals in total.
Work out the number of silver medals.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$

12 AB and CD are parallel to each other.


Find the size of angle $x$.
Give reasons for your answer.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$

13 Here is a cuboid.


All measurements are in centimetres.
$x$ is an integer.
The total volume of the cuboid is less than $1200 \mathrm{~cm}^{3}$
Show that $x<5$
[3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer

14 Five integers have
a mode of 7
a median of 8
a mean of 9 .
What is the greatest possible range of the five integers?
You must show your working.
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer
$15 y$ is directly proportional to the square of $x$.

| $x$ | 2 | 3 | $b$ |
| :---: | :---: | :---: | :---: |
| $y$ | $a$ | 36 | 100 |

Work out the value of $a$ and $b$.
$\qquad$
$\qquad$
$\qquad$
$\qquad$

$$
a=\quad b=
$$

$\qquad$

## 16



Triangle $\mathbf{A}$ is drawn on a coordinate grid.
The triangle $\mathbf{A}$ is reflected in the line $x=1$ and
then enlarged by a scale factor of -1 from the centre $(1,2)$ to give triangle $\mathbf{B}$.
Describe fully the single transformation which maps triangle A onto triangle $\mathbf{B}$.
[4 mark]
$\qquad$
$\qquad$
$\qquad$
$\qquad$

17 Below is a cylinder.


Diagram not drawn accurately
$r: l=1: 3$
Write an expression in terms of $h$, for the volume of the cylinder.
[4 marks]
Write an expression in terms of $h$ for the volume of the cylinder.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer


Not drawn accurately

Circle the size of angle ACD.
$34^{o}$
$53^{\circ}$
$68^{\circ}$
$106^{\circ}$
$146^{\circ}$

19 Write down the equation of the line that is perpendicular to $y=\frac{x}{2}+5$ and passes through $(7,1)$.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer

20 A bag contains counters that are purple, yellow, blue and white.

| Counter | Purple | Yellow | Blue | White |
| ---: | :---: | :---: | :---: | :---: |
| Frequency | 22 | $2 x$ | $x+5$ | $3 x+7$ |

A counter is chosen at random.
The probability the counter is purple is $\frac{11}{50}$.
Work out the probability it is white.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer

21 The diagram below shows a 6-sided shape.
All the corners are right angles.
All the measurements are given in centimetres.


The area of the shape is $40 \mathrm{~cm}^{2}$.
21 (a) Show that $3 x^{2}+17 x-16=0$
$\qquad$
$\qquad$
$\qquad$

21 (b) Solve the equation

$$
3 x^{2}+17 x-16=0
$$

[3 marks]
Give your solutions correct to 3 significant figures.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$ $x=$ $\qquad$

22 An approximate solution to the equation $x^{3}-6 x+3=0$ is found using this iterative process.

$$
x_{n+1}=\frac{\left(3-x_{n}^{3}\right)}{6}
$$

Use this iterative process to find a solution to 3 decimal places of

$$
x^{3}-6 x+3=0
$$

Start with the value $x_{1}=2$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$

23 Rearrange

$$
y=\frac{w x-5}{w-4 x}
$$

to make $x$ the subject.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$

24 ABCDE is a square-based pyramid.
The apex of the pyramid, E , is directly over the centre of the base.


Calculate the volume of the pyramid.
Give your answer correct to 1 decimal place.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer

25


The lengths of the sides of a triangle are $4.5 \mathrm{~cm}, 5.3 \mathrm{~cm}$ and 8.9 cm .
Calculate the size of the largest angle of the triangle.
Give your answer correct to 1 decimal place.
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer

26 Simplify fully

$$
\frac{x^{2}+7 x+12}{4 x-2} \div \frac{x+4}{2}
$$

